

Sheet (2)... Series Resonance

1. A series RLC network has $R=2k\Omega$, $L=40\text{ mH}$, and $C=1\mu\text{F}$. Calculate the impedance at resonance and at one-fourth, one-half, twice, and four times the resonant frequency.

(Ans. $2K$, $2-j0.75K\Omega$, $2-j0.3K\Omega$, $2+j0.3K\Omega$, $2+j0.75K\Omega$).

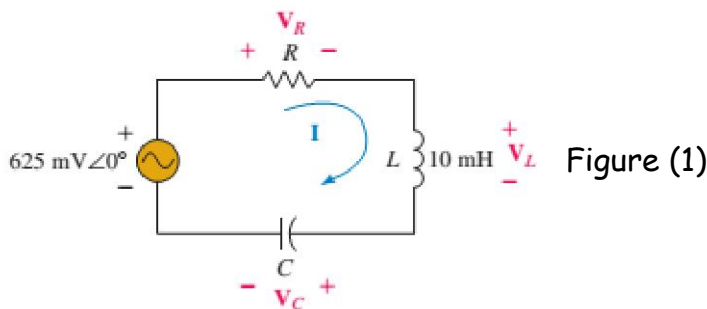
2. A coil with resistance 3Ω and inductance 100 mH is connected in series with a capacitor of 50 pF , a resistor of 6Ω and a signal generator that gives 110 V rms at all frequencies. Calculate ω_0 , Q , and B at resonance of the resultant series RLC circuit.

(Ans. 447.21 krad/s , 4969 , 90 rad/s).

3. Design a series RLC circuit with $B=20\text{ rad/s}$ and $\omega_0=1000\text{ rad/s}$. Find the circuit's Q .

(Ans. = $Q=50$, assume $R=10\Omega$, so $L=0.5\text{H}$, $C=2\mu\text{F}$).

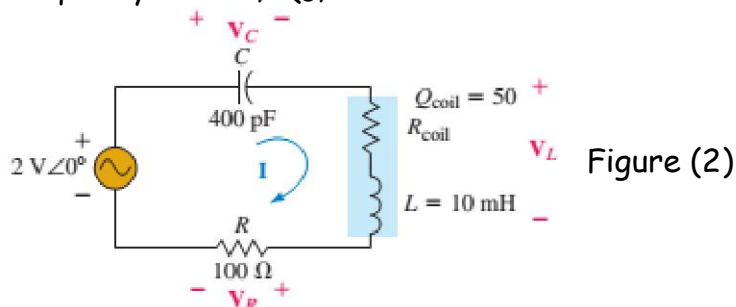
4. Consider the circuit of Figure 1
- Determine the values of R and C such that the circuit has a resonant frequency of 25 kHz and an rms current of 25 mA at resonance.
 - Calculate the power dissipated by the circuit at resonance.
 - Determine the phasor voltages, V_C , V_L , and V_R at resonance.



(Ans. a- $R=25\Omega$, $C=4.05\text{nF}$ /// b- $P=15.6\text{mW}$ /// c- $V_C=39.3\angle-90$, $V_L=39.3\angle 90$, $V_R=0.625\angle 0$)

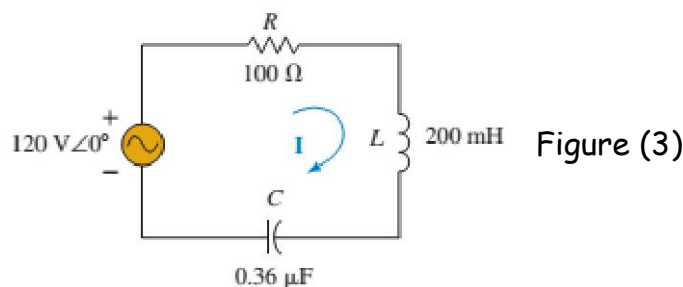


5. Refer to the circuit of Figure 2.
- Determine the resonant frequency expressed as ω (rad/s) and f (Hz).
 - Calculate the total impedance, Z_T , at resonance.
 - Solve for current I at resonance.
 - Solve for V_R , V_L , and V_C at resonance.
 - Calculate the power dissipated by the circuit and evaluate the reactive powers, Q_C and Q_L .
 - Find the quality factor, Q_S , of the circuit.

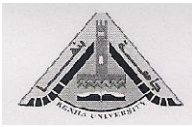


(Ans. a- $\omega_S=500\text{Krad/s}$, $f_S=79.6\text{KHz}$ /// b- $Z_T=200\angle 0$ /// c- $I=10\text{mA}\angle 0$ /// d- $V_R=1\angle 0$, $V_L=50.01\angle 88.85$, $V_C=50\angle -90$ /// e- $P_t=20\text{mW}$ /// f- $Q_S=25$).

6. Refer to the circuit of Figure 3.
- Find ω_S , Q , and BW (in radians per second).
 - Calculate the maximum power dissipated by the circuit.
 - From the results obtained in (a) solve for the approximate half-power frequencies, ω_1 and ω_2 .
 - Calculate the actual half-power frequencies, ω_1 and ω_2 , using the component values and the appropriate equations.



(Ans. a- $\omega_S=3727\text{rad/s}$, $Q=7.45$, $BW=500\text{rad/s}$ /// b- $P_{\text{max}}=144\text{W}$ /// c- $\omega_1=3477\text{rad/s}$, $\omega_2=3977\text{rad/s}$ /// d- $\omega_1=3485.2\text{rad/s}$, $\omega_2=3985\text{rad/s}$)



Home Assignment (1):

1. For the circuit in Fig. 4, find the frequency ω for which $v(t)$ and $i(t)$ are in phase.

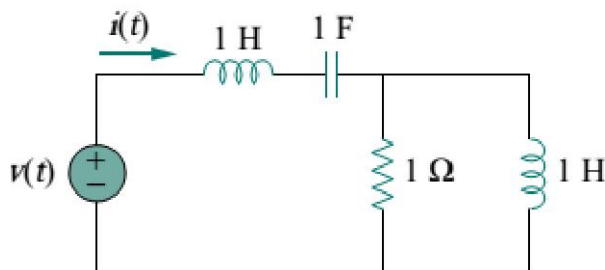


Figure (4)

2. Refer to the series resonant circuit of Figure 5.
 - a. Determine the resonant frequency, ω_S .
 - b. Solve for the input impedance, $Z_T = Z \angle \theta$, of the circuit at frequencies of $0.1 \omega_S$, $0.2 \omega_S$, $0.5 \omega_S$, ω_S , $2 \omega_S$, $5 \omega_S$, and $10 \omega_S$.
 - c. Using the results from (b), sketch a graph of Z (magnitude in ohms) versus ω (in radians per second) and a graph of θ (in degrees) versus ω (in radians per second).
 - d. Using your results from (b), determine the magnitude of current at each of the given frequencies.
 - e. Use the results from (d) to plot a graph of I (magnitude in amps) versus ω (in radians per second).

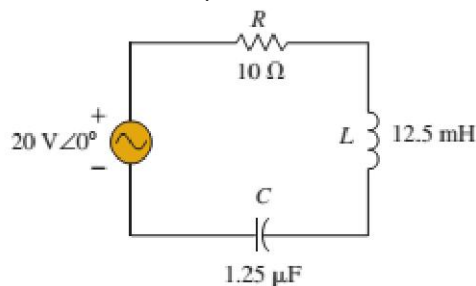


Figure (5)

Good Luck